

Solving Impurity Structures Using Inelastic Neutron Scattering

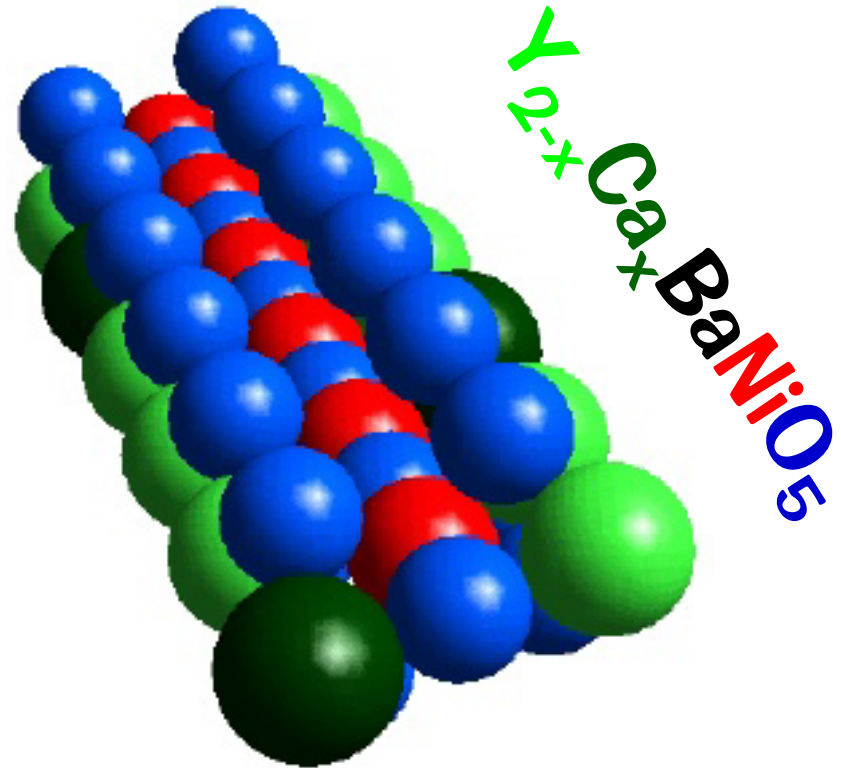
Collin Broholm*

Johns Hopkins University and NIST Center for Neutron Research

Quantum Magnetism

- Pure systems
- vacancies
- bond impurities

Conclusions



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D. H. Reich, Guangyong Xu, and I. Zaliznyak
Physics and Astronomy, Johns Hopkins University

G. Aeppli, M. E. Bisher, and M. M. J. Treacy
NEC Research Institute

J. F. DiTusa
Physics and Astronomy, Louisiana State University

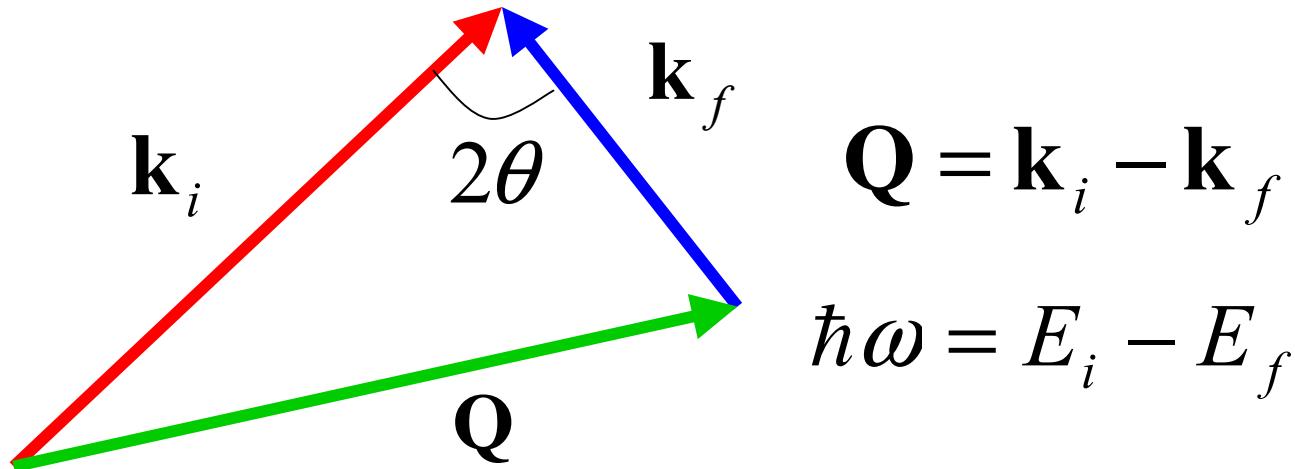
R. L. Paul
National Institute of Standards and Technology

C. D. Frost
ISIS Facility Rutherford Appleton Laboratory

T. Ito K. Oka
Electrotechnical Laboratory, Japan

H. Takagi
ISSP, University of Tokyo

Inelastic Neutron Scattering

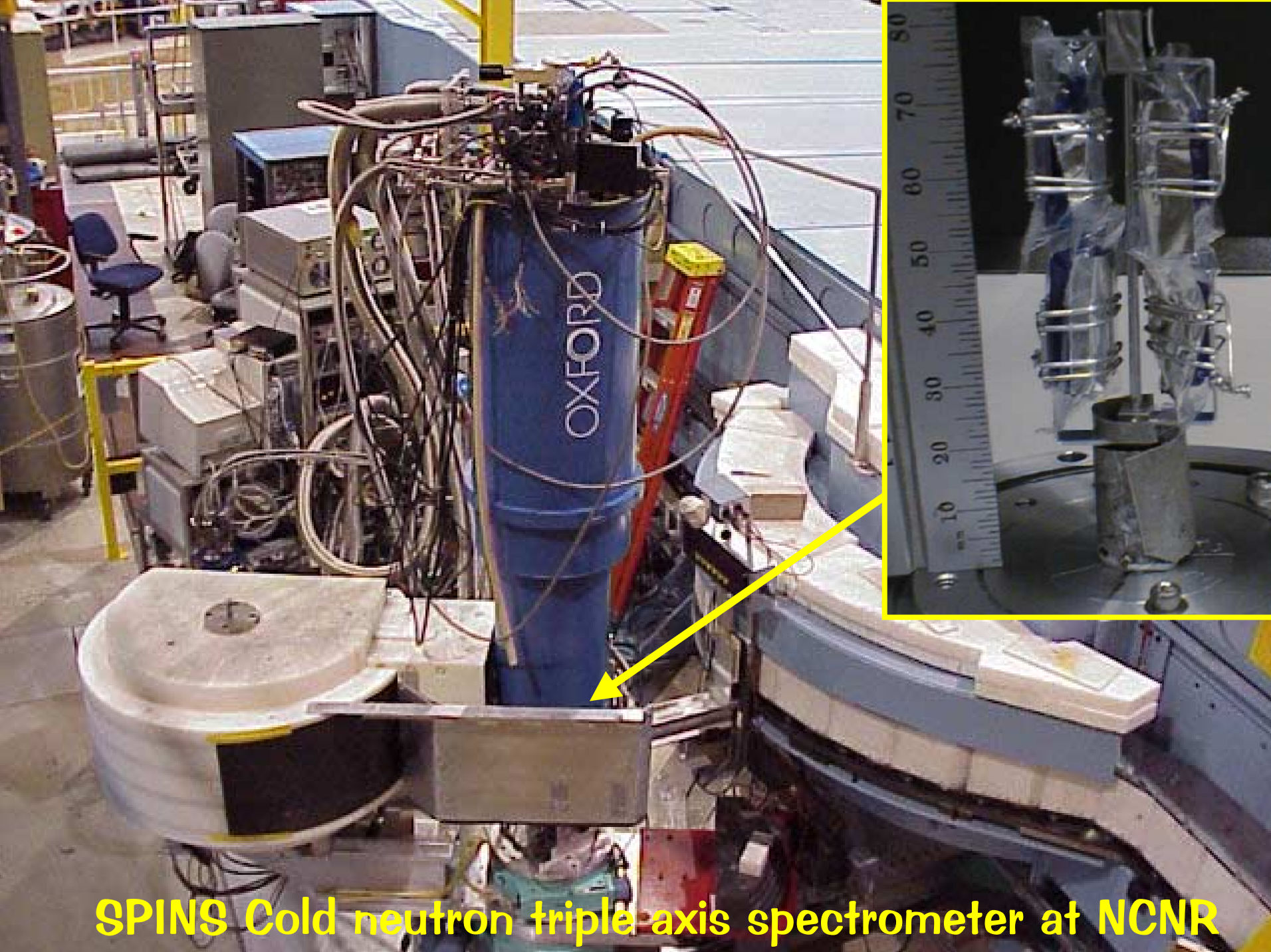


Nuclear scattering

$$S(\mathbf{Q}, \omega) = \frac{1}{2\pi\hbar} \int dt e^{-i\omega t} \frac{1}{N} \langle \rho_{\mathbf{Q}}(0) \rho_{-\mathbf{Q}}(t) \rangle$$

Magnetic scattering

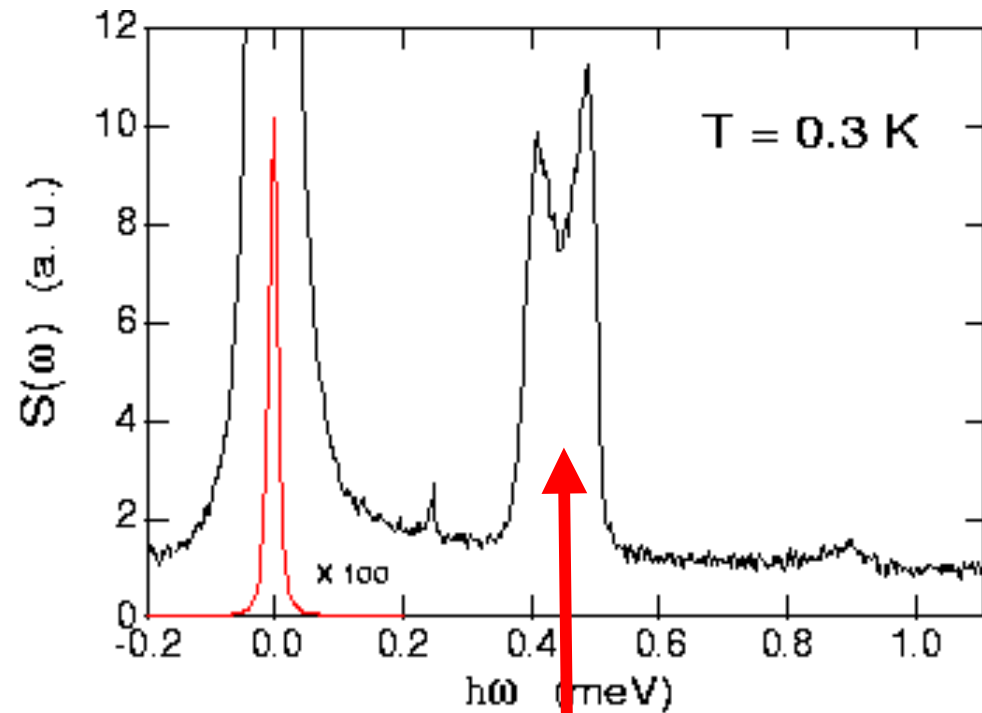
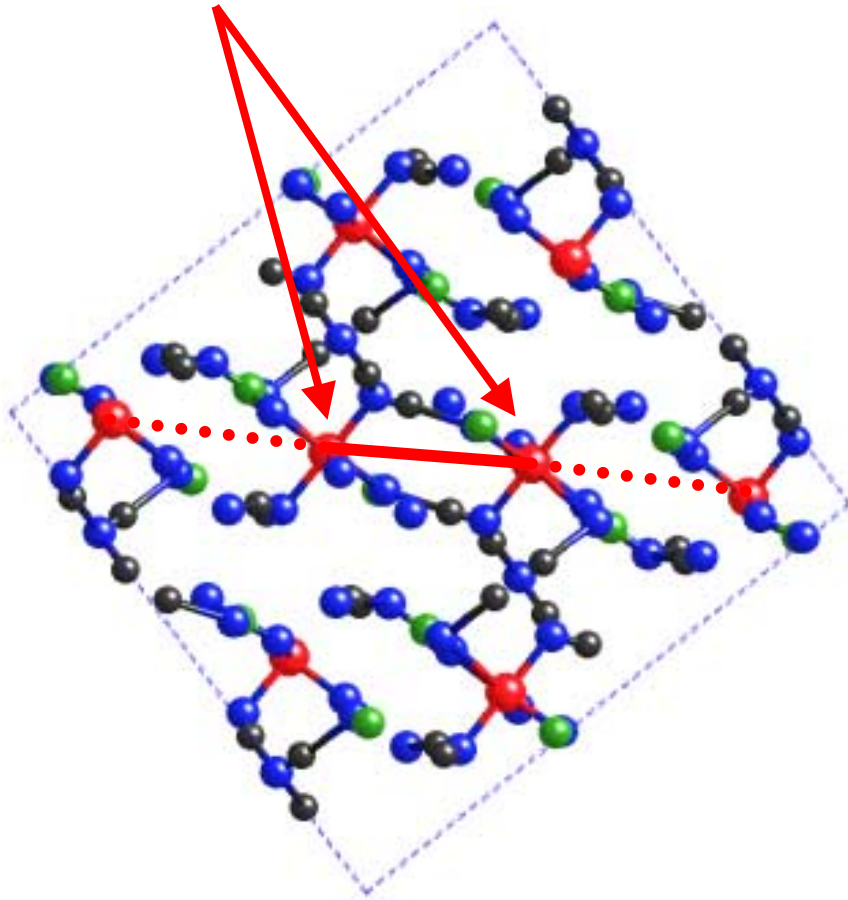
$$S^{\alpha\beta}(\mathbf{Q}, \omega) = \frac{1}{2\pi\hbar} \int dt e^{-i\omega t} \frac{1}{N} \sum_{\mathbf{R}\mathbf{R}'} e^{i\mathbf{Q}\cdot(\mathbf{R}-\mathbf{R}')} \langle S_{\mathbf{R}}^{\alpha}(0) S_{\mathbf{R}'}^{\beta}(t) \rangle$$



SPINS Cold neutron triple axis spectrometer at NCNR

Simple example of "Quantum" magnet

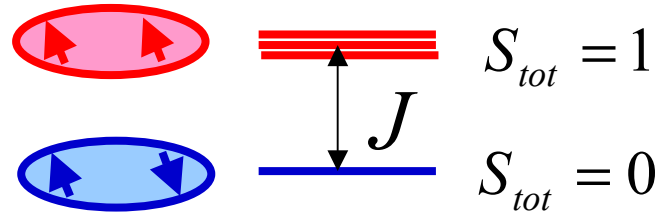
Cu(NO₃)₂·2.5D₂O : dimerized spin-1/2 system



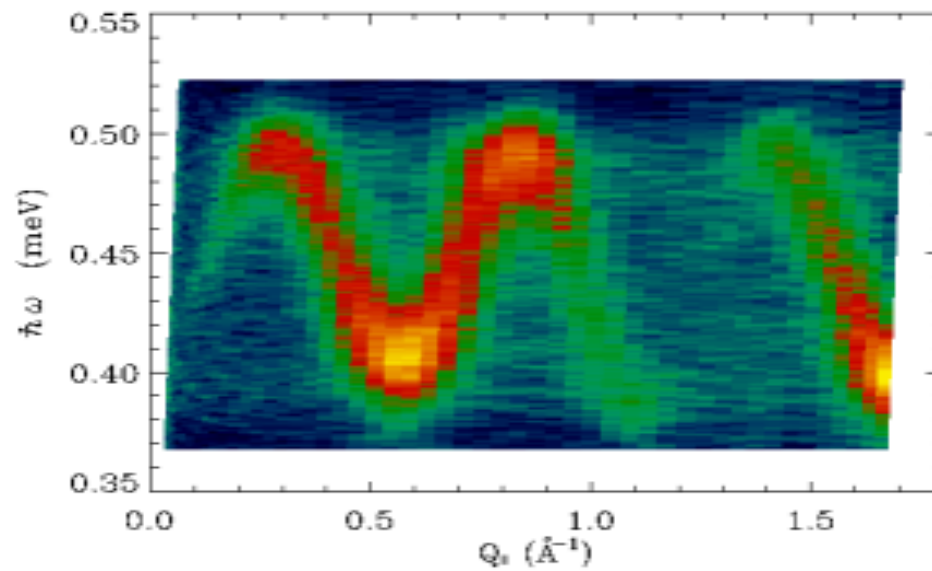
**Only Inelastic
magnetic scattering**

Why dimerized chain is a spin liquid

- A spin-1/2 pair with AFM exchange has a singlet - triplet gap:



- inter-dimer coupling allows triplet propagation as can be seen from the dispersion of the singlet triplet transition



Types of Quantum magnets

- Definition: small or vanishing frozen moment at low T:

$$|\langle \mathbf{S} \rangle| \ll S \quad \text{for } k_B T \ll J$$

- Conditions that yield quantum magnetism

- Low effective dimensionality

- Low spin quantum number

- geometrical frustration

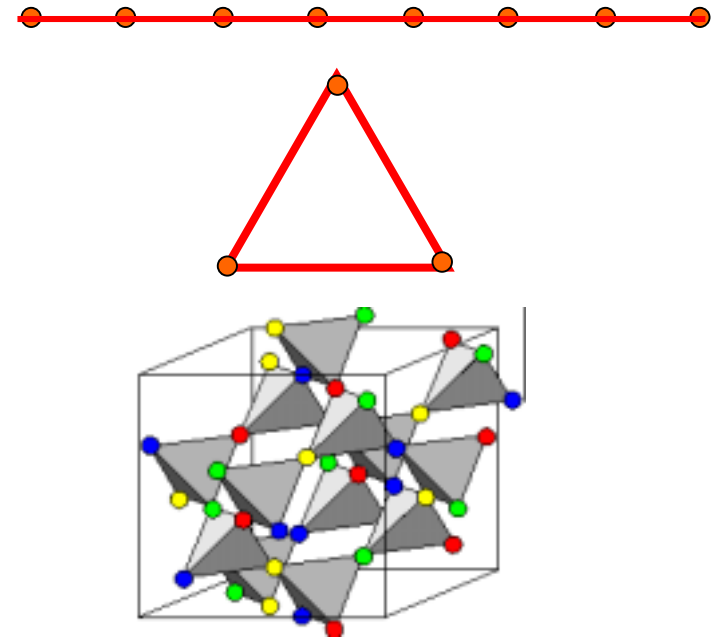
- dimerization

- weak connectivity

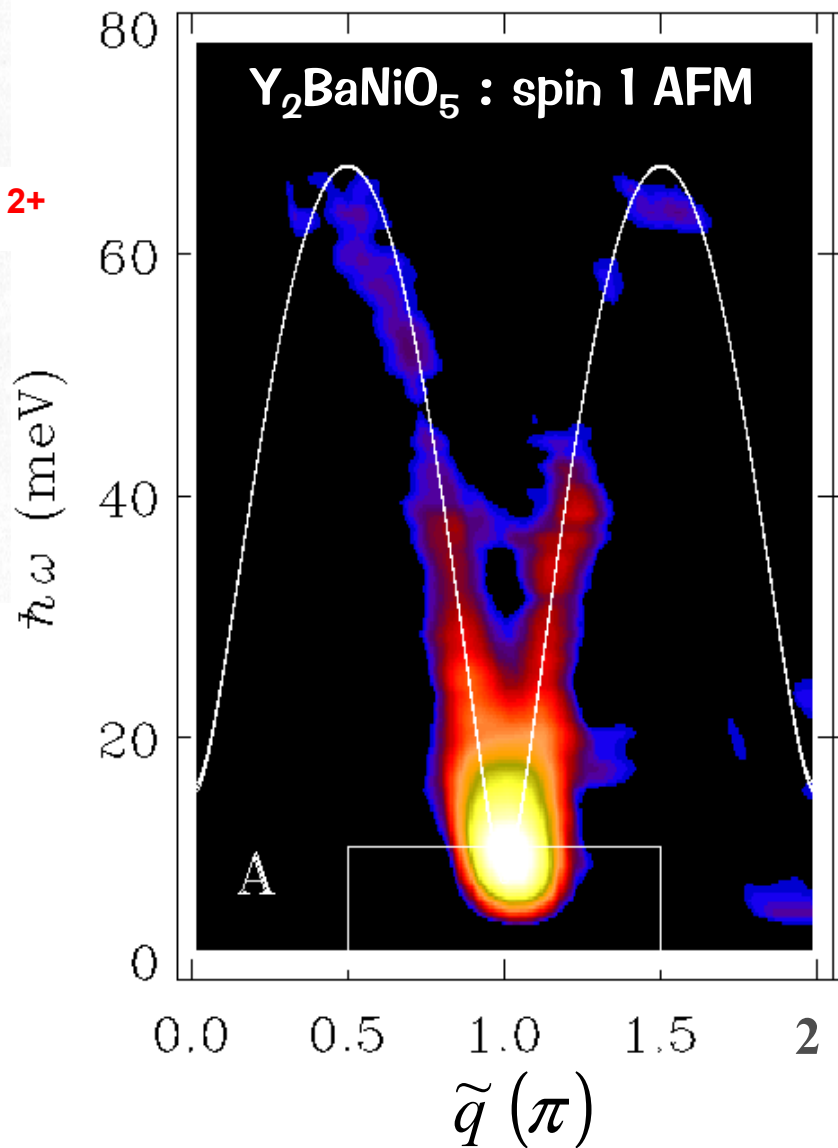
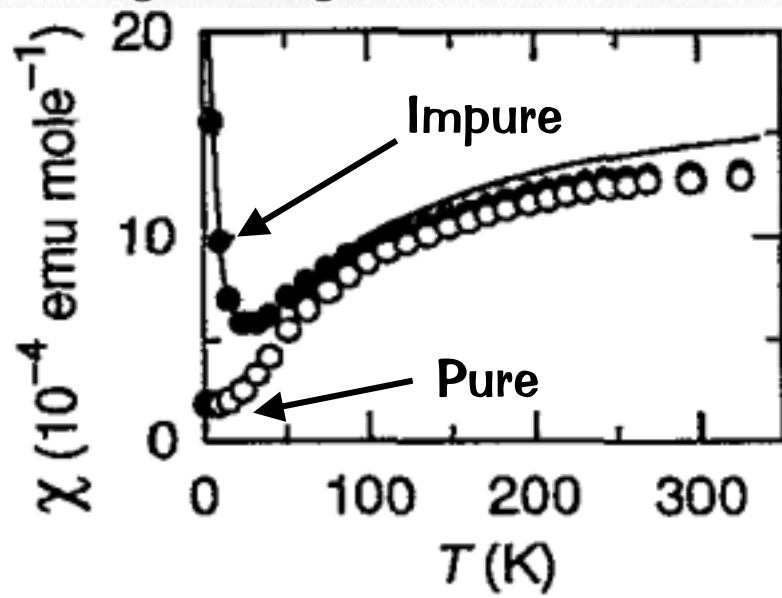
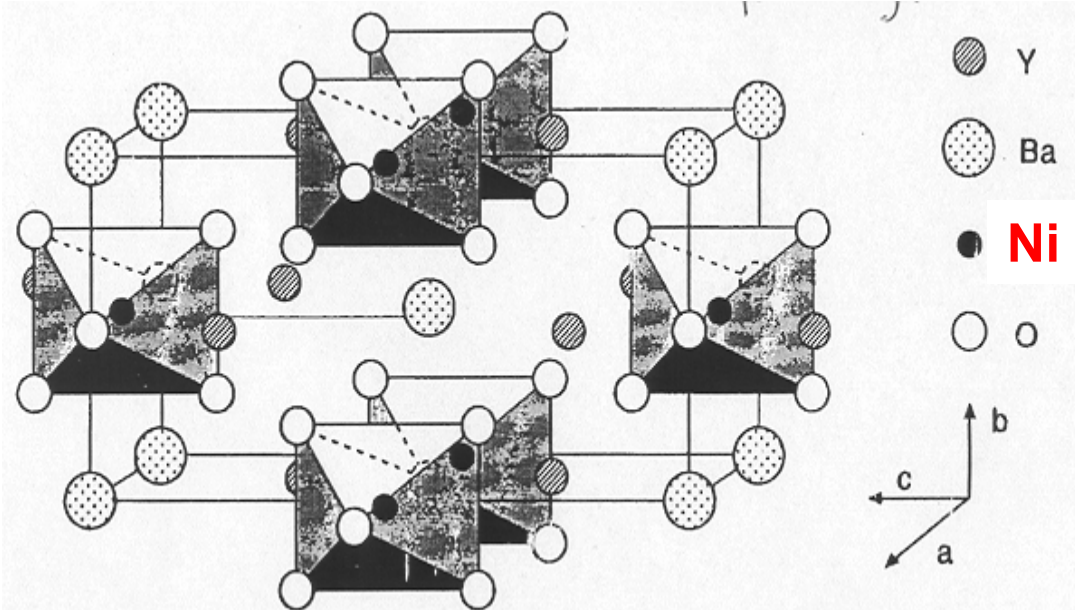
- interactions with fermions

- Novel coherent states

- impurities can induce magnetic polarons

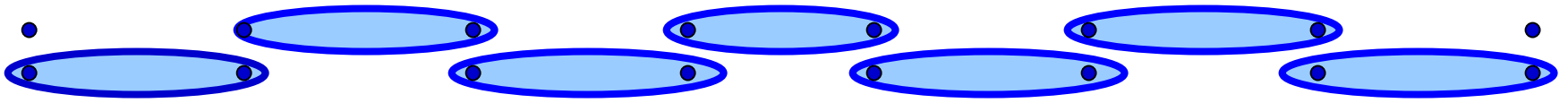


One dimensional spin-1 antiferromagnet Y_2BaNiO_5



Macroscopic singlet ground state of $S=1$ chain

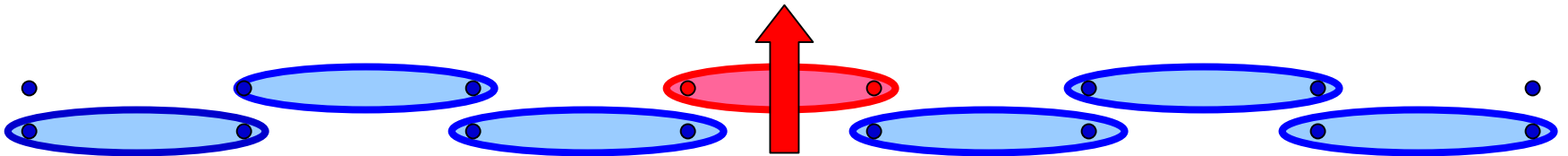
- Magnets with $2S=nz$ have a nearest neighbor **singlet covering** with full lattice symmetry.



- This is exact ground state for spin projection Hamiltonian

$$\mathcal{H} = \sum_i P_i(S_{tot} = 2) = \sum_i \left(\mathbf{S}_i \cdot \mathbf{S}_{i+1} - \frac{1}{3} (\mathbf{S}_i \cdot \mathbf{S}_{i+1})^2 \right) \approx \sum_i \mathbf{S}_i \cdot \mathbf{S}_{i+1}$$

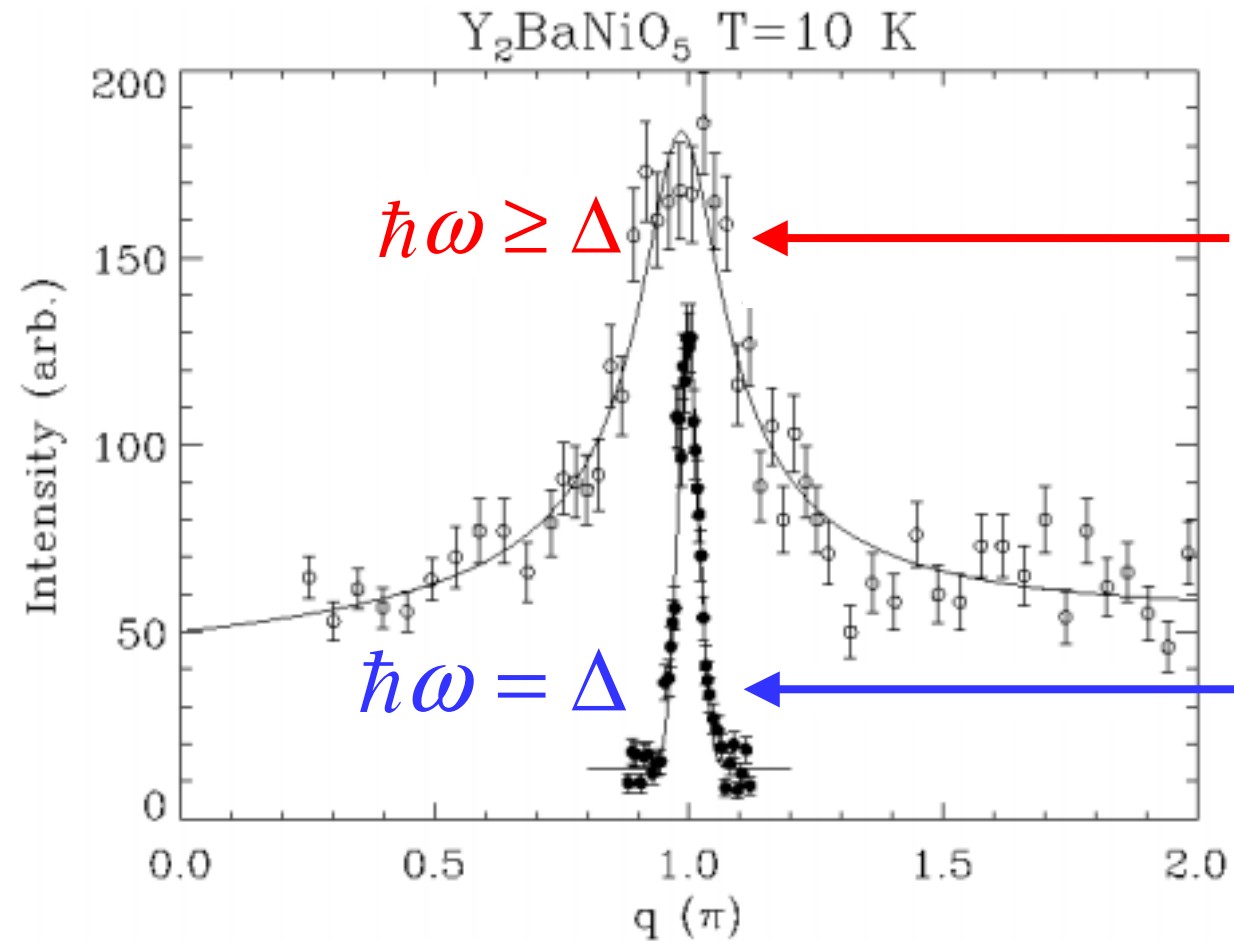
- Excited states are **propagating bond triplets** separated from the ground state by an energy gap $\Delta \approx J$.



Haldane PRL 1983

Affleck, Kennedy, Lieb, and Tasaki PRL 1987

Coherence in a fluctuating system

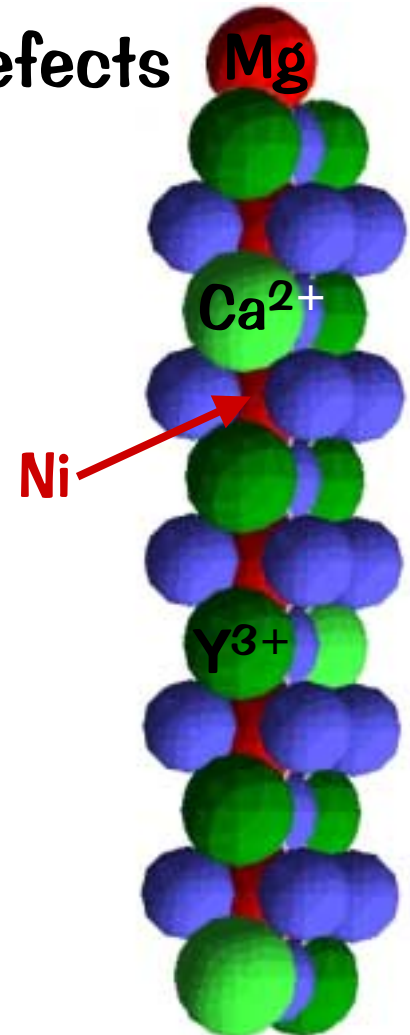
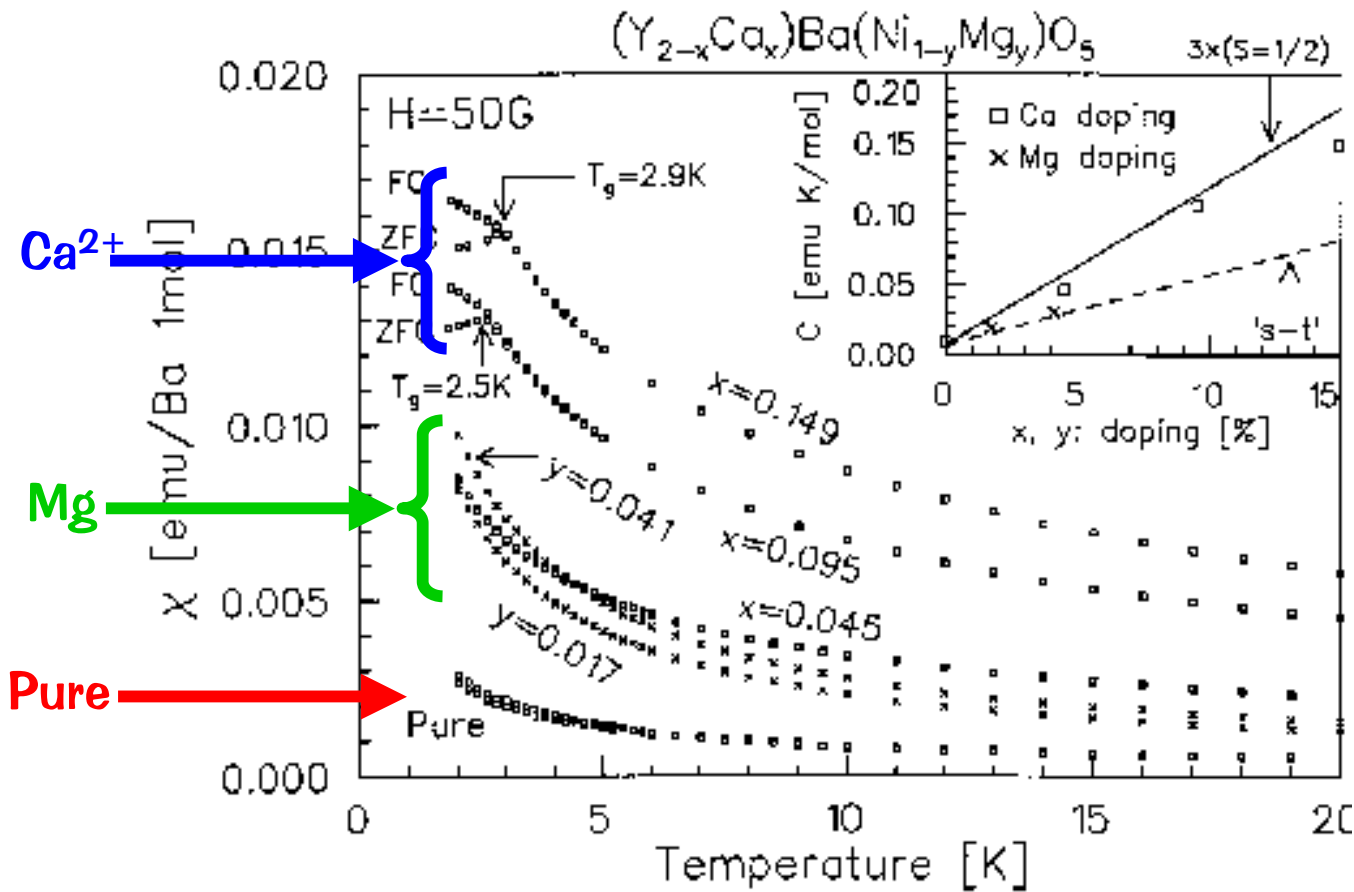


Short range G.S. spin correlations

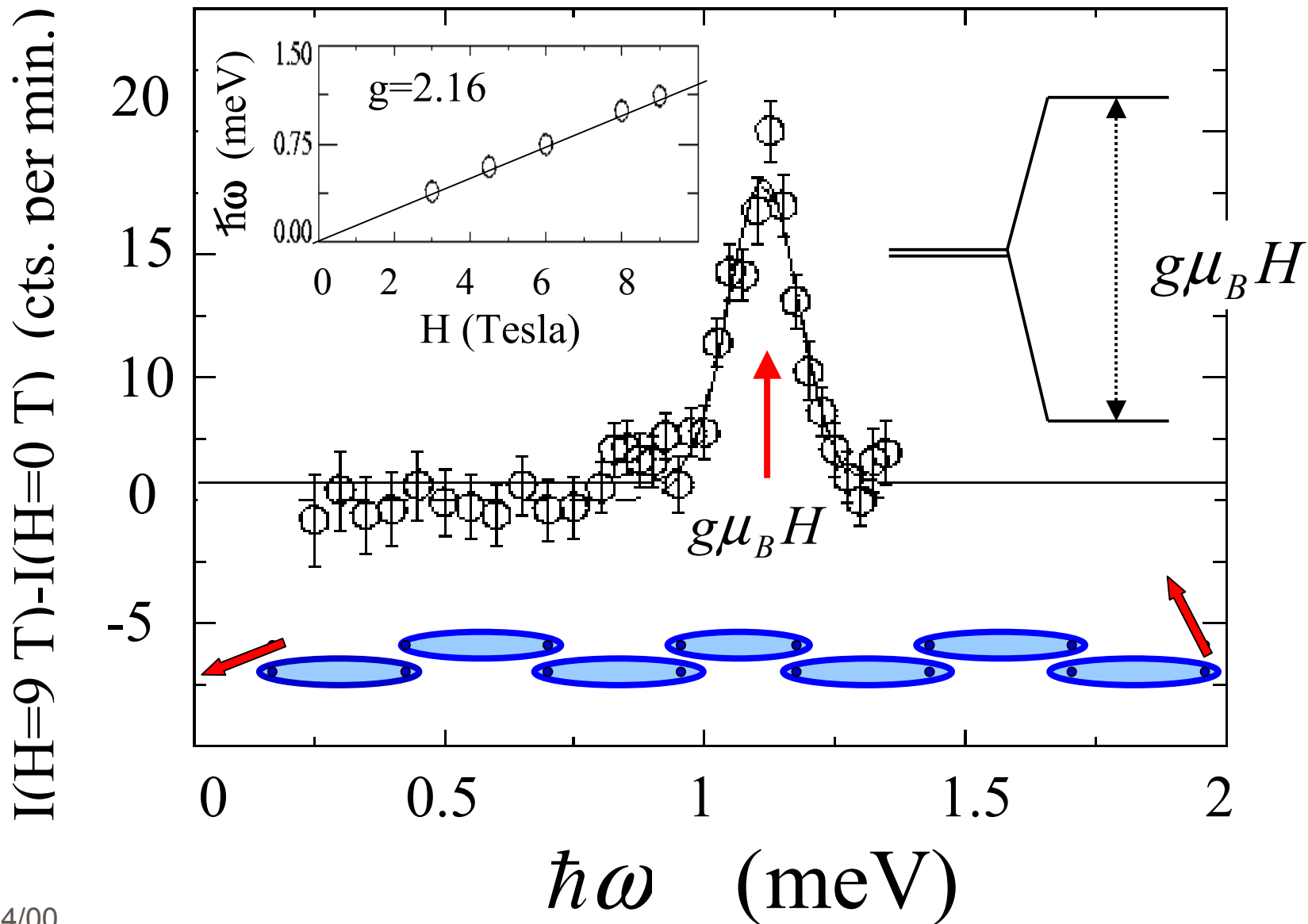
Coherent triplet propagation

Impurities in Y_2BaNiO_5

- Mg^{2+} on Ni^{2+} sites \rightarrow finite length chains
- Ca^{2+} on Y^{3+} sites \rightarrow mobile bond defects

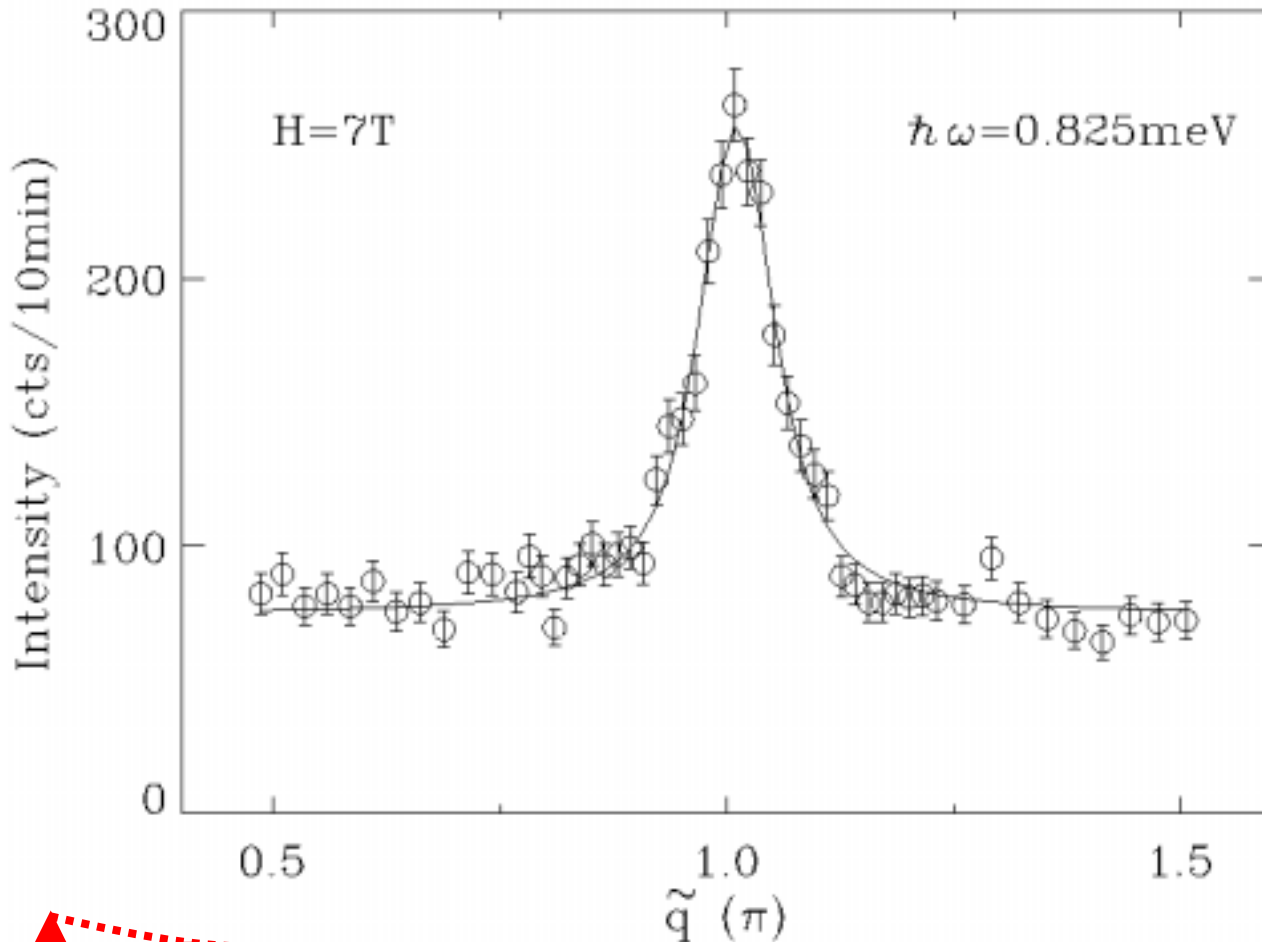


Zeeman resonance of chain-end spins



Form factor of chain-end spins

$Y_2BaNi_{1-x}Mg_xO_5$ $x=4\%$ $\hbar\omega = g\mu_B H$

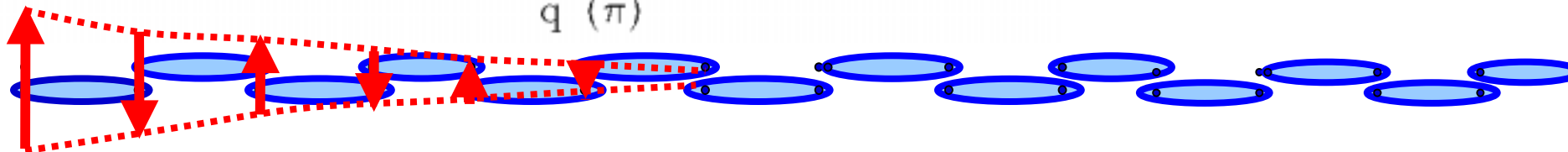


Q-dependence reveals that resonating object is AFM.

The peak resembles $S(Q)$ for pure system.



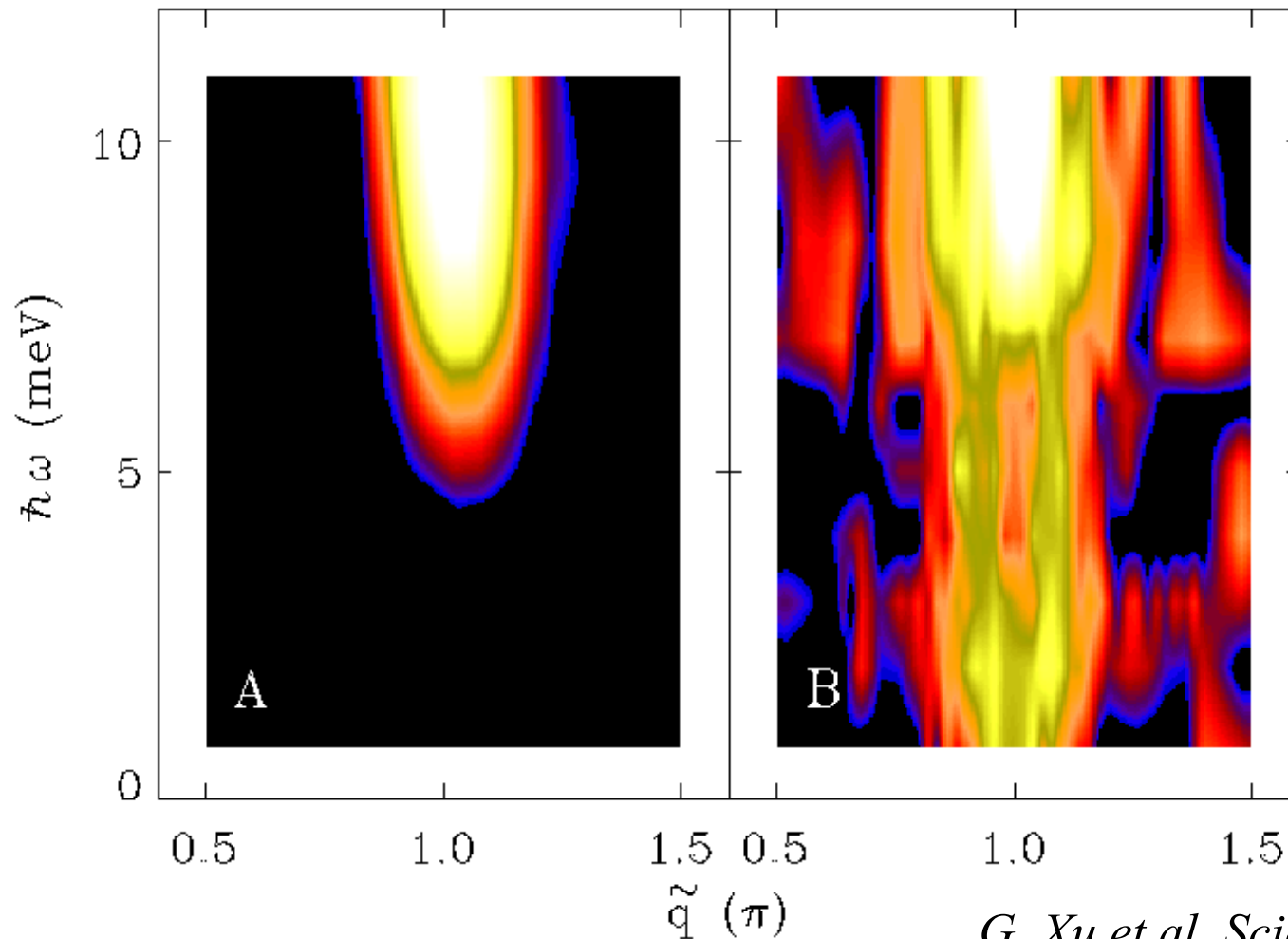
Chain end spin carry AFM polarization cloud of length $\xi \approx 7$ Ni-Ni spacings



Sub gap excitations in Ca-doped Y_2BaNiO_5

Pure

9.5% Ca



$\text{Y}_{2-x}\text{Ca}_x\text{BaNiO}_5$:

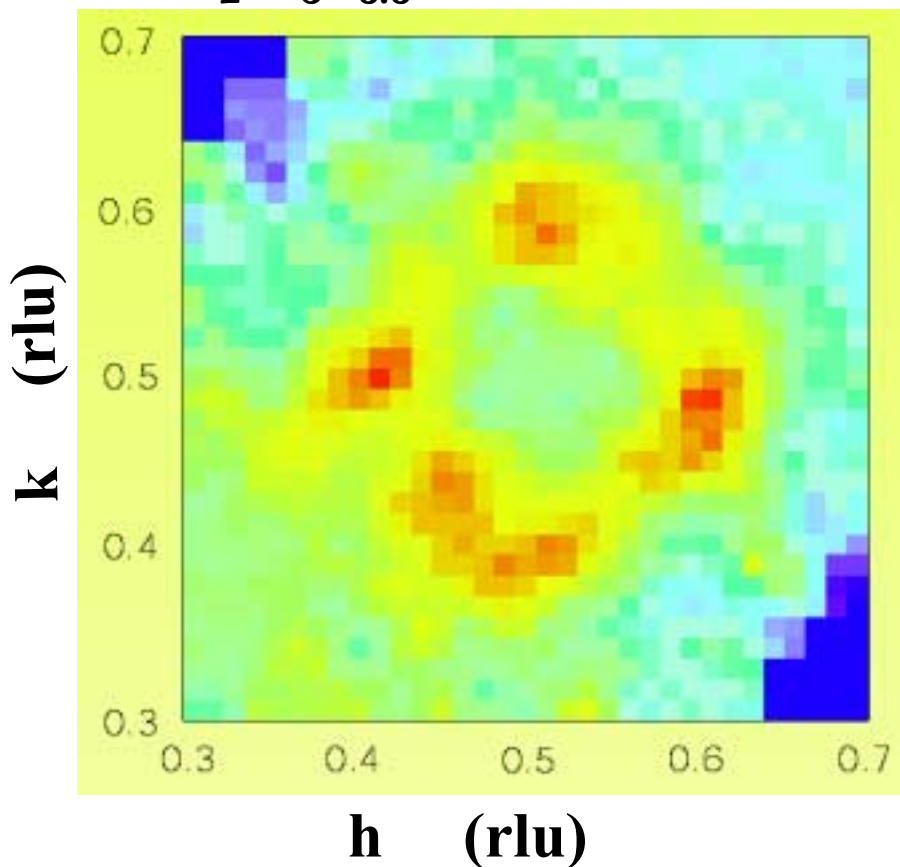
- Ca-doping creates states below the gap
- sub-gap states have doubly peaked structure factor

G. Xu et al. Science (2000)

Incommensurate modulations in high T_c superconductors

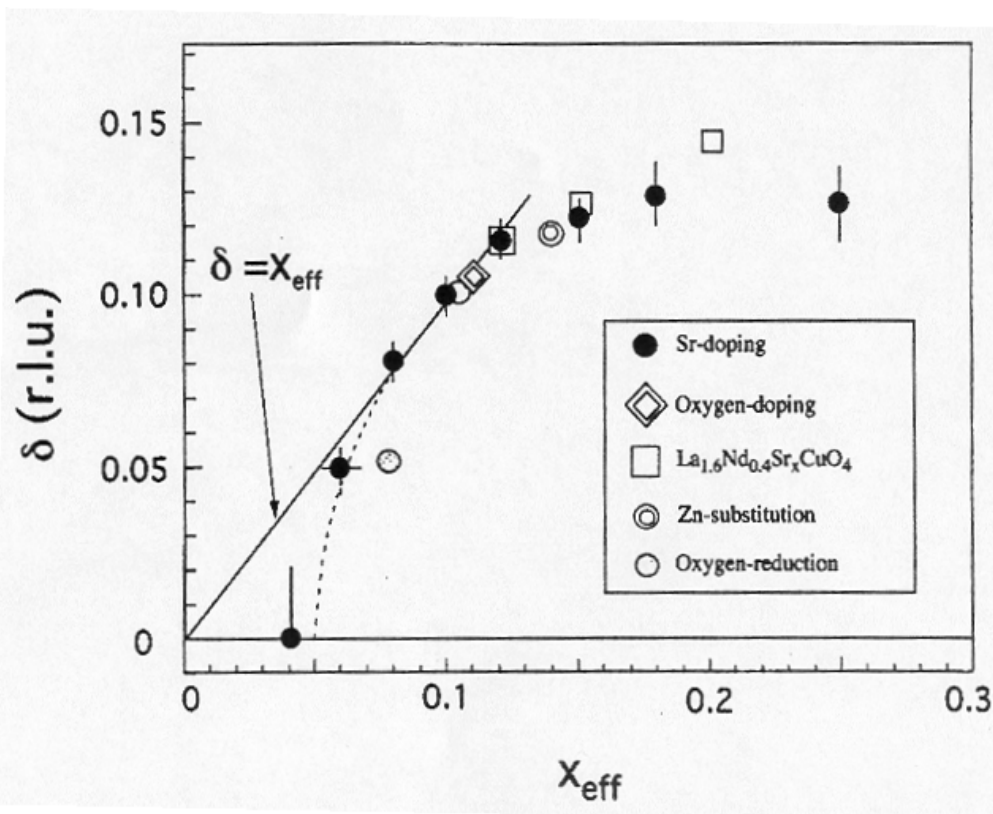


$\text{YBa}_2\text{Cu}_3\text{O}_{6.6}$ $T=13$ K $E=25$ meV



Hayden et al. (1998)

$\text{La}_{2-x}\text{Sr}_x\text{CuO}_4$



Yamada et al. (1998)

Origin of incommensurate peaks in doped systems

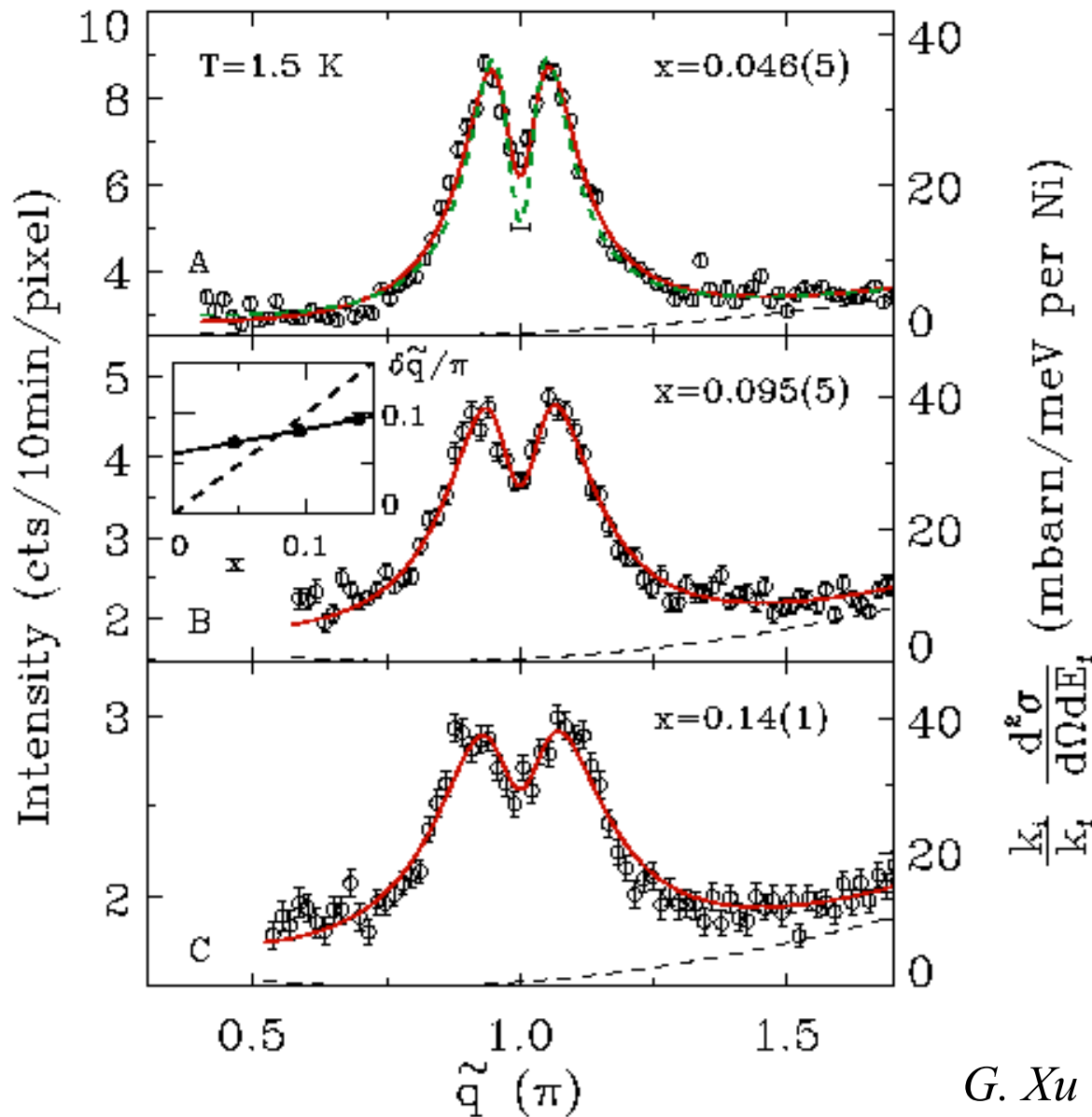
$$\delta q \propto x$$

- Charge ordering yields incommensurate spin order
- Quasi-particle Quasi-hole pair excitations in Luttinger liquid

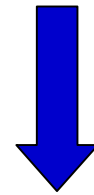
δq indep. of x

- Single impurity effect

Does δq vary with calcium concentration?

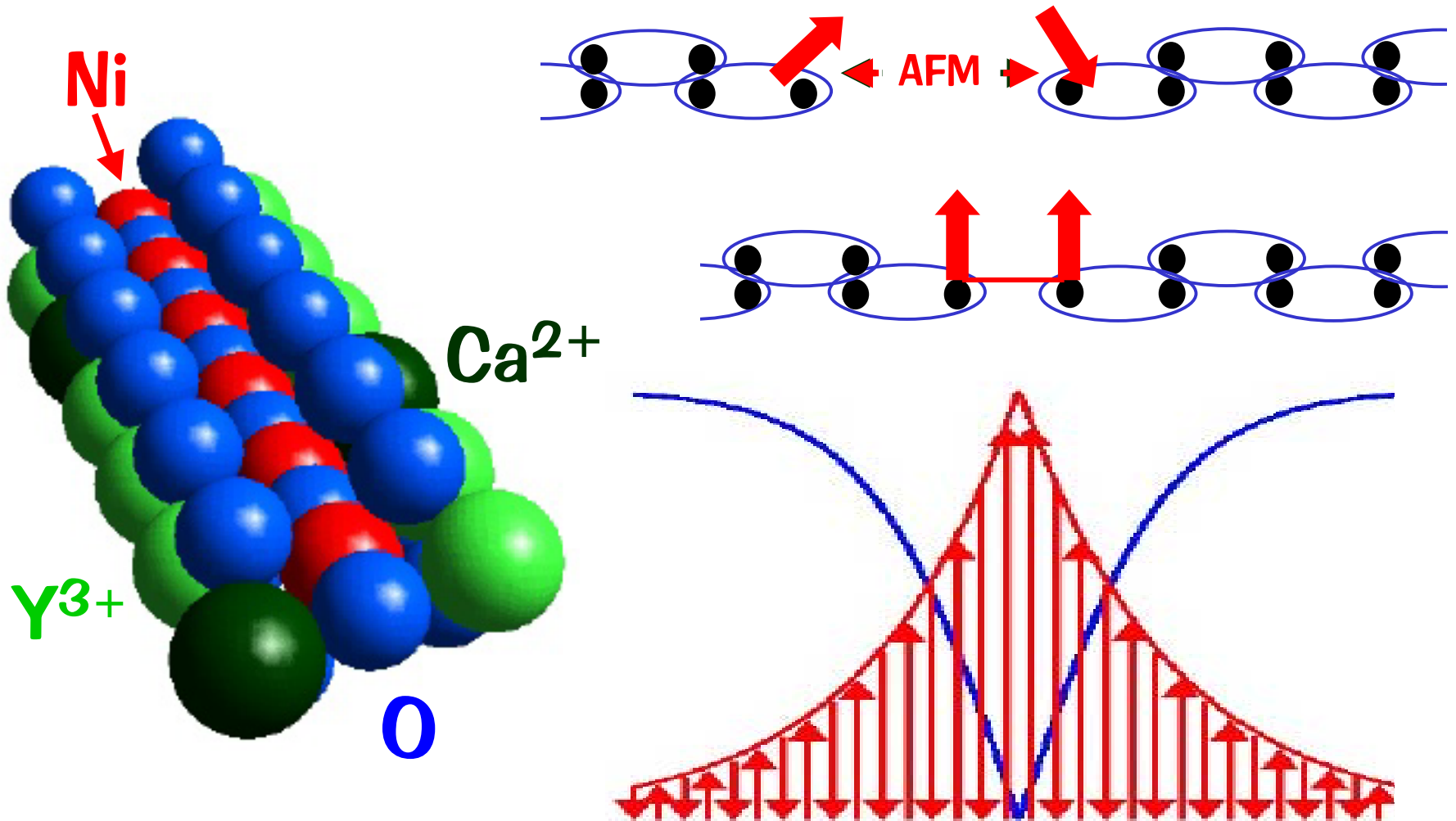


δq not strongly dependent on x

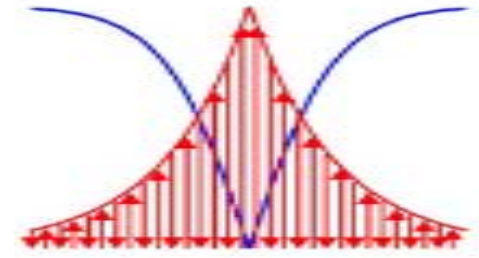
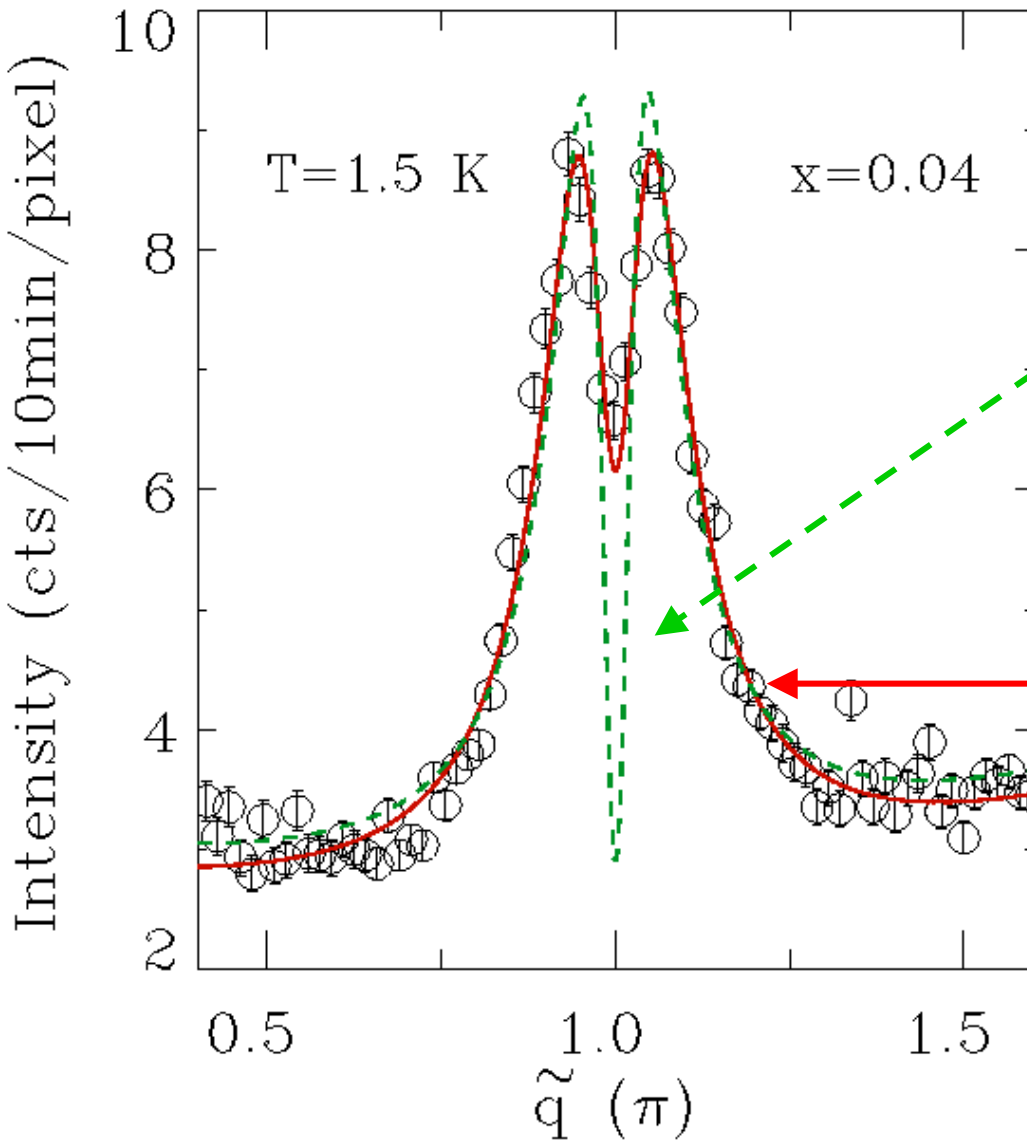


single impurity effect

Bond Impurities in a spin-1 chain: $Y_{2-x}Ca_xBaNiO_5$



Form-factor for FM-coupled chain-end spins

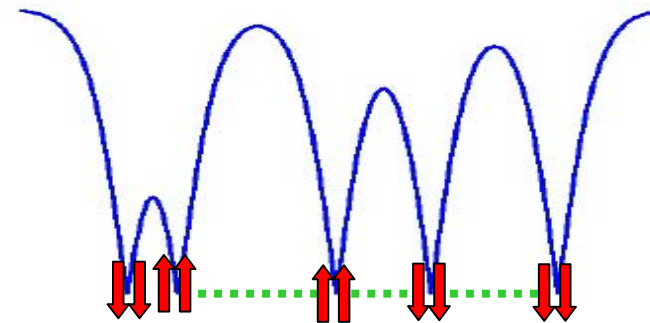


A symmetric AFM droplet

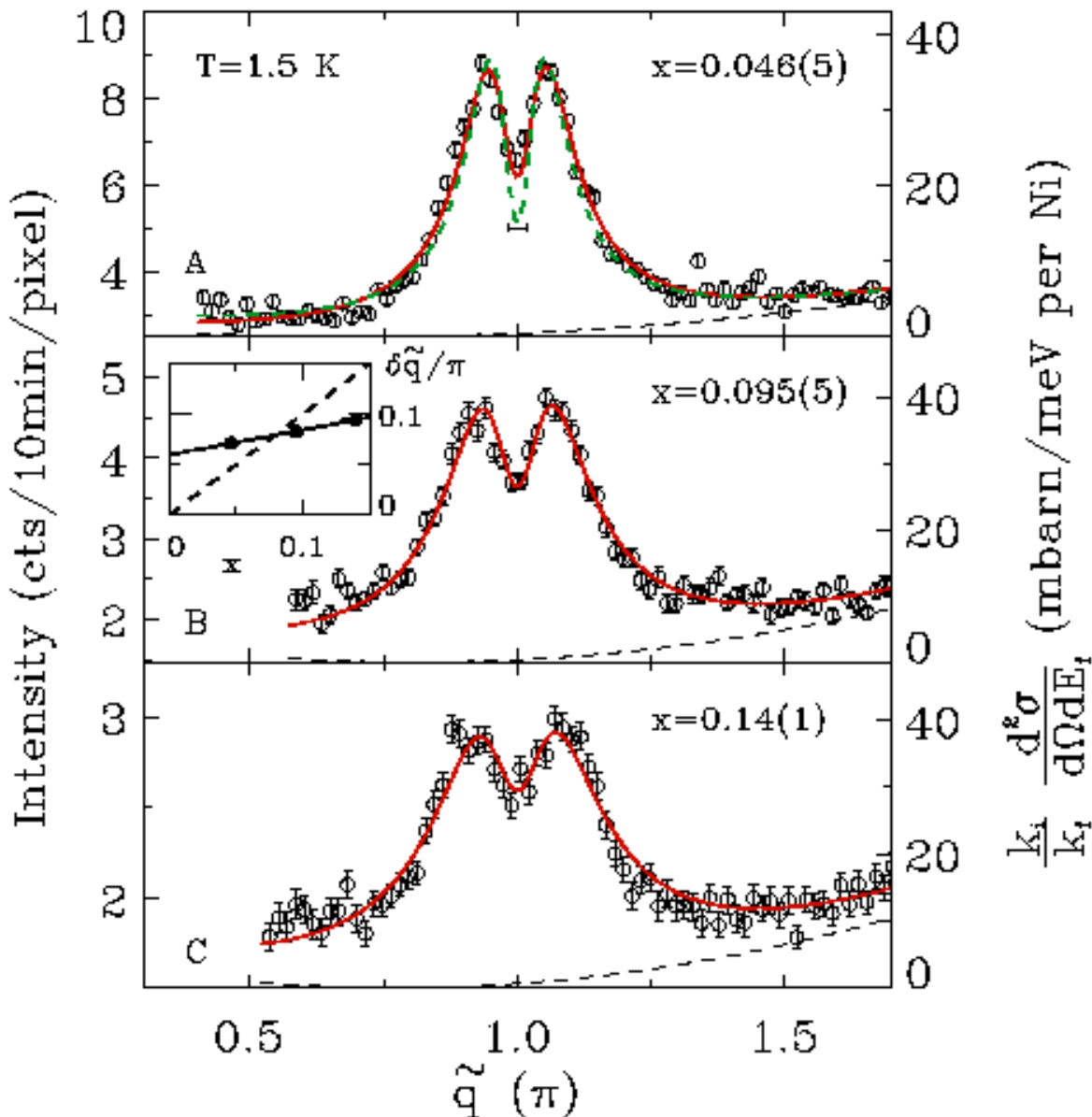
$$S(q) = 2 \operatorname{Re} \left\{ M_{\infty}(q) e^{iq/2} \right\}$$

Ensemble of independent randomly truncated AFM droplets

$$S(q) = \sum_{l,l'} P_{ll'} \left| M_l(q) e^{iq/2} + M_{l'}^*(q) e^{-iq/2} \right|^2$$



Consistent description for all concentrations



Parameters:

- background
- amplitude
- droplet size **7.6(5)**

Conclusions

■ Quantum Magnets

- low dimensional frustrated and/or weakly connected
- Coherent low T states rather than magnetic order
- Challenging to describe because fluctuations are essential

■ Impurities in spin-1 chain

- They create sup-gap composite spin degrees of freedom
- Edge states have extended AFM wave function
- Holes create AFM spin polaron with phase shift π

■ Probing impurities with neutrons

- Spectroscopic separation yields unique sensitivity to impurity structures (in quantum magnets) through coherent diffuse inelastic neutron scattering